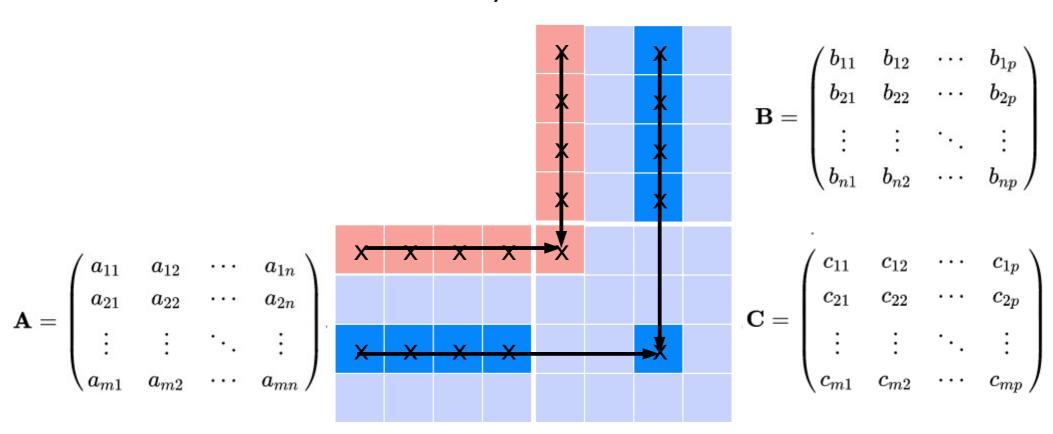


# GPU for Deep Learning Optimized Matrix Multiplication

Elisabeth Brunet

#### C = AB

Given two matrices A and B,



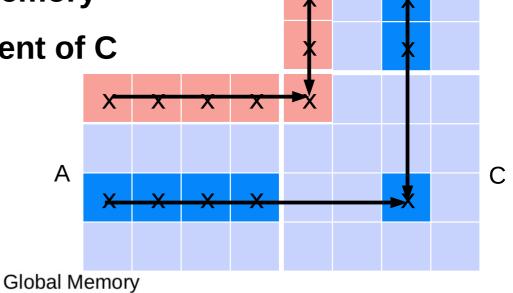
• Such that  $c_{ij}=a_{i1}b_{1j}+a_{i2}b_{2j}+\cdots+a_{in}b_{nj}=\sum_{k=1}^n a_{ik}b_{kj},$ 

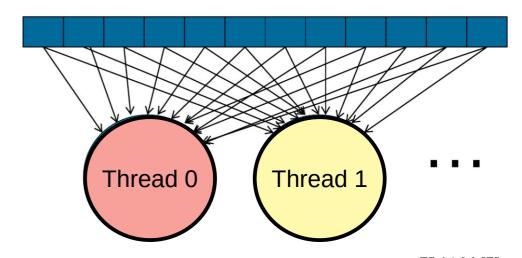


# 1)Basic algorithm

- Matrices A, B and C in global memory
- Each thread calculates an element of C
- Each thread accesses
  - to a whole line of A
  - and a whole column of B

- Data access
   non-aligned and scattered
  - Coalescing problem
- Repeated data access

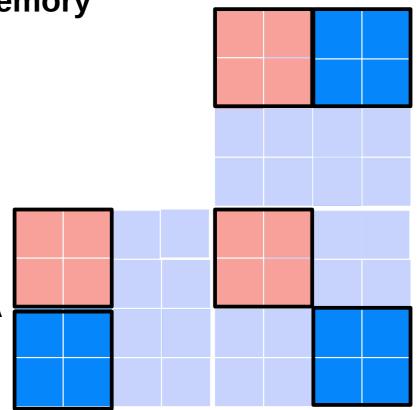






# 2) Tiled algorithm

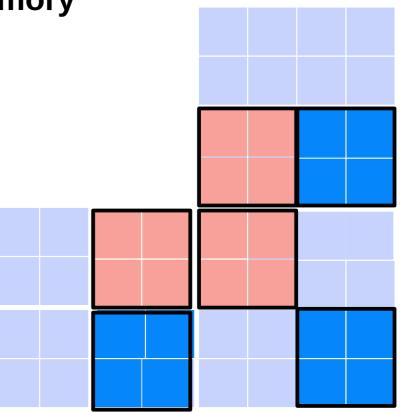
Iterative algorithm
 on sub-matrixes multiplication
 treated by a block fiting in shared memory





## 2) Tiled algorithm

Iterative algorithm
 on sub-matrixes multiplication
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#### 2) Tiled algorithm

Iterative algorithm
 on sub-matrixes multiplication
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#### Iteration in 4 steps :

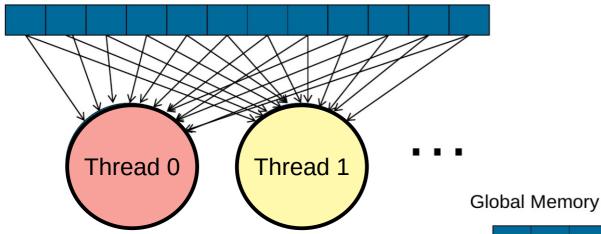
- (a) Cooperative loading of a data in tiles in shared memory
- (b) Synchronization to ensure that data are loaded
- (c) Calculation of partial results by threads on loaded data
- (d) Synchronization before changing the data of the tiles for the next iteration



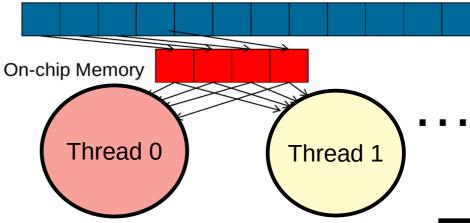
# (a) Cooperative data loading

Objective : change the access pattern

**Global Memory** 



- → Regular access to global memory
- + Quick access once in shared memory !!!





# (a) Cooperative data loading

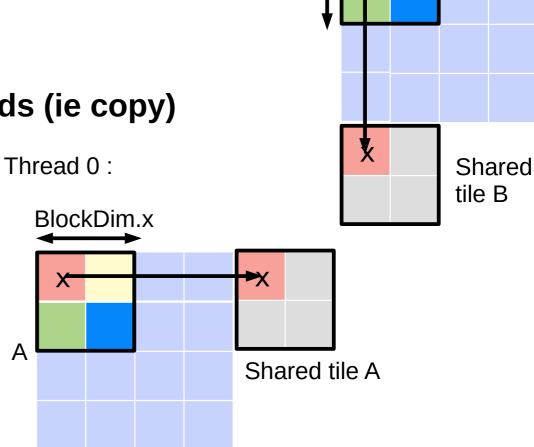
- Sub-tiles of BLOCKSIZE\*BLOCKSIZE elements
  - BLOCKSIZE = sqrt(1024) = 32

Each thread of the block loads (ie copy)

an element from A

and an element from B

into the shared tiles

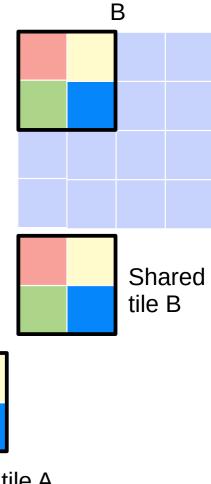


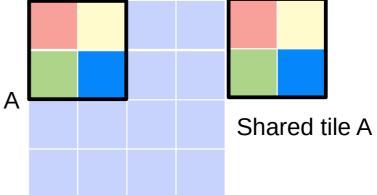
BlockDim.y



## (b) Synchronization!

Once the barrier passed,
 the two sub-tiles are complete

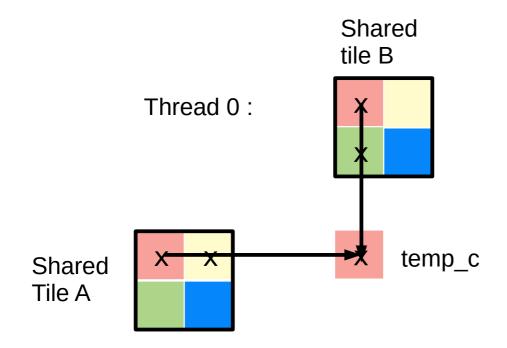






#### (c) Partial result computation

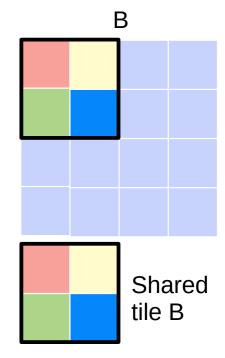
- Multiplication of matrices on current tiles
- Accumulation in a scalar variable stored in a register

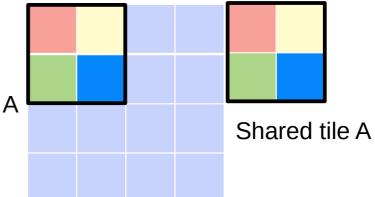




#### (d) Synchronization!

Once the barrier passed,
 all the threads of the block have finished to compute
 and the two sub-tiles can be modified







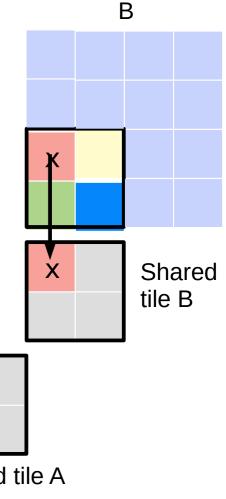
#### Switch to the next tile

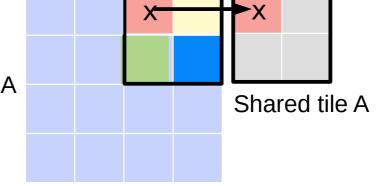
(a) Cooperative data loading

in the **SAME** shared tile

- (b) Synchronization
- (c) Accumulation of the partial result in local variable temp c Thread 0:
- (d) Synchronization

al result B Thread 0 :



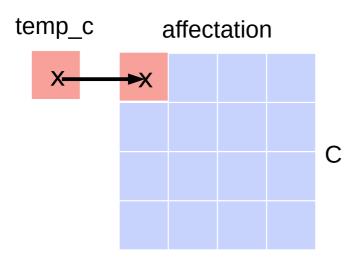




#### Final result

Assignment of the result in the C matrix remaining in global memory

#### Thread 0:





#### To go further,

#### Each partial result could be computed by another block

- Additional dimension on the grid to identify the tile to be treated
- Reduction of the partial results :
  - Atomic operation for accumulation: atomicAdd
  - Reduction on the GPU thanks to a kernel
  - Reduction on the CPU



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- A lot of different optimizations and strategies
  - → Field of research in itself
- Best algorithms in the cuBLAS library



# Last detail: access to a matrix element

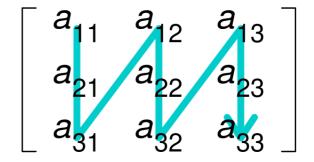
#### Matrix organization

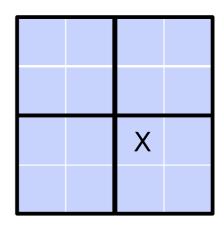
- = one-dimensional vector column major
  - Colum major required by cuBLAS

#### Access to an element in 2 steps

- 1) Projection of the grid of threads on the matrix
  - Line = blockldx.y \* blockDim.y + threadIdx.y
  - Column = blockldx.x \* blockDim.x + threadIdx.x
- 2) Linearization in the data structure in one column-major dimension
  - A[column \* nbLineOfA+ line]
  - Given macro IDX2C : #define IDX2C(i,j,nb\_rows) (((j)\*(nb\_rows))+(i))

#### Column-major order







# Let's go to practise now!

